

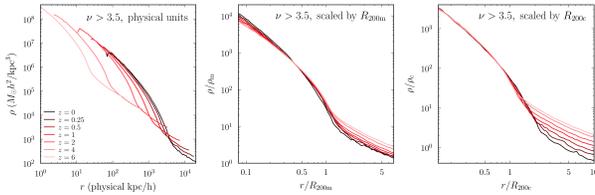
# Are halo profiles and concentrations universal?

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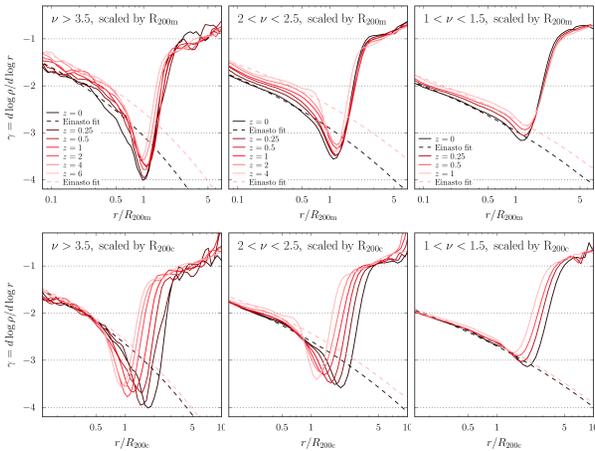
[ Profiles: 1401.1216 - Concentrations: 1407.4730 ]

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## Are halo density profiles universal?



**Figure 1:** The median density profiles of very massive halos of fixed  $\nu$  at different redshifts. In physical units (left), the profiles vary across redshifts. When radii are rescaled by some spherical overdensity radius,  $R_{\Delta}$ , and the corresponding reference density,  $\rho_m$  or  $\rho_c$ , the inner density profiles become nearly universal.



**Figure 2:** The exact redshift scaling is easier to see in the logarithmic slope of the density profiles, shown here for three bins in peak height which, at  $z=0$ , correspond to very massive clusters ( $M > 10^{15} M_{\odot}/h$ , left), more common clusters ( $M \sim 10^{14} M_{\odot}/h$ , center), and galaxy to group scale halos ( $M \sim 10^{12-13} M_{\odot}/h$ , right). The radii are scaled by  $R_{200m}$  in the top row and by  $R_{200c}$  in the bottom row. **The inner region ( $r < R_{200c}$ ) is most self-similar in units of  $R_{200c}$ , whereas the outer region ( $r > R_{200m}$ ) is most self-similar in units of  $R_{200m}$ .** Scaling with  $R_{vir}$  and  $\rho_{vir}$  gives intermediate results. The self-similarity of the inner (outer) regions in units of  $R_{200c}$  ( $R_{200m}$ ) holds for all halo masses, not only the most massive clusters. The steepening of the profiles around  $R_{200m}$  in massive halos is caused by their higher accretion rate (see Diemer & Kravtsov 2014a for details).

## Abstract

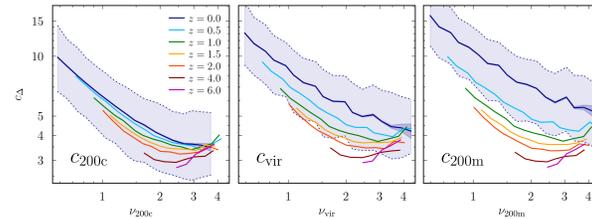
Numerous theoretical arguments and simulation results indicate that the density profiles of halos are closely related to their mass assembly history. The latter is expected to be a universal function of peak height,  $\nu = \delta_c / \sigma(M)$ . Thus, we expect that the density profiles of halos with a fixed  $\nu$  are close to universal, as long as radii and densities are expressed in the proper units.

We analyze a large suite of cosmological simulations to test how well this expectation holds in a hierarchical cosmology. We find that at fixed  $\nu$ , the inner density profiles are most universal in units of  $R_{200c}$ , while the outer profiles are most universal in units of  $R_{200m}$ , where a radius  $R_{\Delta}$  is defined to enclose an overdensity  $\Delta$  wrt. the mean or critical density of the universe. In addition, Figure 2 demonstrates that the outer profiles are not universal, but exhibit a systematic variation with  $\nu$ . This variation is caused by the different mass accretion rates of halos.

We also show that the relation between concentration,  $c$ , and  $\nu$  is most universal when  $c$  is defined as  $c_{200c} = R_{200c} / r_s$ . However, sizeable deviations from universality in the  $c_{200c}$ - $\nu$  relation remain. We show that these deviations can be explained as a residual dependence of concentration on the local slope of the matter power spectrum,  $n$ . We construct a universal function of only two variables,  $c_{200c}(\nu, n)$ , that accurately describes concentrations across 22 orders of magnitude in mass and over a wide range of redshifts and cosmologies.

## Are halo concentrations universal?

Concentration exhibits a non-trivial dependence on mass, redshift, and cosmological parameters. However, it has been shown that the relation between  $c$  and peak height,  $\nu$ , is almost universal with redshift (e.g., Prada et al. 2012).

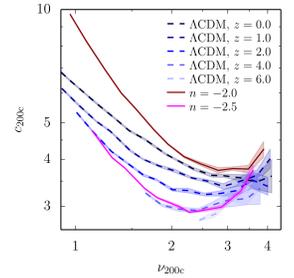


**Figure 3:** The  $c$ - $\nu$  relation for three definitions of the virial radius. Clearly, the  **$c_{200c}$ - $\nu$  relation is most universal with redshift**, while the other definitions,  $c_{vir}$  and  $c_{200m}$ , experience a spurious evolution at low redshift, namely when dark energy becomes important and  $\rho_m$  or  $\rho_c$  diverge. This evolution is related to the density profiles shown in Figure 2: at low  $z$ , halos are mostly in the slow accretion regime (e.g., Zhao et al. 2003), meaning that  $r_s$  barely changes, and  $c_{\Delta} = R_{\Delta} / r_s \sim R_{\Delta}$ . As we show on the left, the inner parts of density profiles at fixed  $\nu$  are most universal in redshift when radii are rescaled by  $R_{200c}$ , leading to a more universal  $c_{200c}$ - $\nu$  relation.

## A universal model for halo concentrations

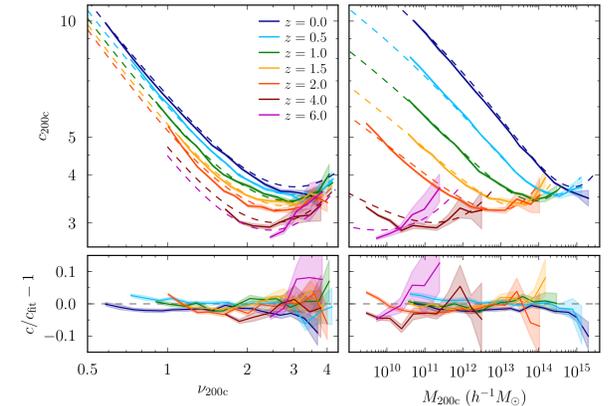
The concentration-peak height relation is almost universal with redshift, but not quite (see center column). Thus, we are looking for a second parameter besides  $\nu$  that affects concentration.

**Figure 4:** The  $c$ - $\nu$  relation in two self-similar cosmologies with  $\Omega_m=1$  and power-law spectra of slopes  $n=-2$  and  $n=-2.5$ . Clearly,  $n$  has a large impact on concentration. The  $\Lambda$ CDM relations lie in between  $n=-2$  and  $n=-2.5$ , roughly the range of  $n$  in a  $\Lambda$ CDM power spectrum.



Thus, we postulate that  $n$  is a second parameter influencing concentration, and that **concentration can be expressed as a universal function,  $c(\nu, n)$** . We fit our simulations results with such a function, namely a double power-law whose normalization and location of the minimum vary with  $n$ .

**Figure 5:** With only seven free parameters, this model fits  $\Lambda$ CDM concentrations to about 5% accuracy from  $z=0$  to  $z=6$  (the solid lines show simulation results, the dashed lines our model). The model also describes the concentrations in self-similar cosmologies, as well as those of Earth-mass halos at  $z=30$ . We provide a python code to evaluate our model at [www.benediktdiemer.com/code](http://www.benediktdiemer.com/code).



## References

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